Infrared intensity parameters of the diacetylene and acidity of acetylenic hydrogens

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Abstract—Preferred signs of the dipole moment derivatives of the diacetylene have been determined by using G-sum rule graph and molecular orbital calculations. Atomic polar tensors and effective charges of the diacetylene are reported. The hydrogen effective charge calculated from the atomic polar tensor ($\xi_{\rm H} = 0.369e$) is in excellent agreement with that obtained from G-sum rule graph ($\xi_{\rm H} = 0.371e$). MNDO calculations on the H(C=C)_nH (n = 1, 2, 3, 4 and 5) series indicate that the hydrogen effective charge increases with increasing number of C=C units. This is due to the magnitude of the $\partial p_z/\partial z_{\rm H}$ polar tensor element, as a consequence of the increasing charge flux along the series. Finally, this element seems to be a good indicator of the intrinsic acidity of acetylenic protons.

INTRODUCTION

Hydrogen effective charges obtained from infrared intensities show that these values in acetylenic compounds are much larger than those found in saturated hydrocarbons, aromatic compounds and carbon-carbon double bonded molecules [1]. Basically, this can be associated to the greater acid character of these hydrogens bonded directly to carbon-carbon triple bond [2]. In this sense, one question which is particularly interesting is what happens with the hydrogen effective charge along a homologous series such as $H(C \equiv C)_n H$. Would the hydrogen be progressively more acid?

The first molecule of this series, acetylene, HC_2H , has been the subject of numerous spectroscopic investigations [3], whereas the second, diacetylene, HC_4H , only recently was the object of an ample study on its experimental force field and infrared fundamental intensities [4]. Although the fundamental intensities of the diacetylene have been reduced to dipole moment derivatives with respect to symmetry coordinates, $(\partial \mathbf{p}/\partial S_j)$, the atomic polar tensors and effective charges have not been reported. Furthermore, the signs of the $\partial \mathbf{p}/\partial Q_i$'s have not been tested by G-sum rule graph and quantum chemical calculations. All these aspects and also the effect of the substituent ($\mathbf{R}-\mathbf{C}\equiv\mathbf{C}-\mathbf{H}$; $\mathbf{R}=\mathbf{H}$, CCH, CH₃ and CN) on the intrinsic acidity of the acetylenic proton are the basic targets of this paper.

RESULTS AND DISCUSSION

Diacet ylene

The fundamental intensities of the diacetylene were initially reported by POPOV *et al.* [5] for the C_4H_2 species, except to the band relative to C-C=C deformation. Recently, KOOPS *et al.* [4] remeasured all the C_4H_2 intensities and also C_4D_2 ones. The intensities reported by POPOV *et al.* are in very good agreement with these recent measurements within the experimental error, except the one related to the CH stretching band by a factor of ~ 2 . The reason for this large discrepancy is not clear. Nevertheless, the measured intensities by KOOPS *et al.* reveal an internal consistency by applying the *F*-sum rule [4], in contrast with those from POPOV *et al.*

Here we make use of the G-sum rule [6] in its graphical representation, to analyse simultaneously the fundamental intensities of the diacetylene and to determine the preferred signs of their $\partial \mathbf{p}/\partial Q_i$ from the isotopic invariability of the atomic effective charge. Since the diacetylene has zero permanent dipole moment, the rotational corrections to the Σ_u^+ and Π_u symmetry species are zero. The G-sum rule equation for C₄H₂ and C₄D₂ can be expressed as:

$$(2\xi_{c_2}^2 + 2\xi_{c_3}^2)/m_c = -[x/m_{\rm H} + (2-x)/m_D]\xi_{\rm H}^2 + (1/K)\sum A_i$$
(1)

where x is the number of hydrogen atoms.

In Fig. 1 G-sum rule graph is shown for the Σ_{u}^{+} symmetry species. Firstly it is important to note that using the intensities measured by POPOV *et al.* for C₄H₂ and those by KOOPS *et al.* for C₄D₂ there is no intersection of the intensity pair of lines in the positive quadrant. Since the squares of the effective charges must be positive for all atoms, this is to be expected if the experimental intensity data are reasonably accurate. This is in fact true for the intensities measured by KOOPS *et al.* [4].

The Σ_{u}^{+} symmetry species have two infrared active modes and the signs of the $\partial p_{z}/\partial Q_{i}$ (i = 4 and 5) are easily established from the G-sum rule graph. Since the hydrogen effective charge is invariant to isotopic substitution, the preferred set of signs of the $\partial p_{z}/\partial Q_{i}$'s are obviously (+ -) for C₄H₂ and (+ +) for C₄D₂. Note that these sets of signs fall within the region defining isotopically invariant effective charge values.



Fig. 1. The G intensity sum rule graph for the Σ_{u}^{+} symmetry species of diacetylene.

These sets of signs are identical to those chosen by KOOPS *et al.* [4] through the residual determined from the least-squares fitting procedure in the experimental intensities. However, in this procedure it is necessary to include all intensity data, whereas by the G-sum rule graph, one can determine separately the signs of the $\partial \mathbf{p}/\partial Q_i$ for each symmetry species, without the intensity data from the other symmetry species.

From these sets of signs of $\partial \mathbf{p}/\partial Q_i$ we obtain the dipole moment derivatives with respect to internal coordinates, $(\partial \mathbf{p}/\partial R_k)$, using the usual relation [7],

$$\mathbf{P}_{R} = \mathbf{P}_{O} \mathbf{L}^{-1} \mathbf{U} \tag{2}$$

where the force field, the internal and symmetry coordinates, the geometry and the coordinate system used in this procedure were taken from Ref. 4. The $\partial \mathbf{p}/\partial R_K$ values thus obtained are given in Table 1, whose signs are identical to those obtained from quantum chemical calculations. These were carried out at two levels: *ab initio* 4-31G calculations using the HONDO program [8] and MNDO [9] semiempirical molecular orbital calculations.

In Fig. 2, the G-sum rule graph is shown for the two infrared active bands of the Π_u symmetry species. We have for each molecule only two possible sets of signs for the $\partial \mathbf{p}/\partial Q_i$'s $(\partial p_x/\partial Q_8$ and $\partial p_x/\partial Q_9$), (++) and (+-), taking into account the absence of rotational correction. The preferred set of signs obtained by

Table 1. Experimental and theoretical dipole moment derivatives of the Σ_{u}^{+} symmetry species of $C_{4}H_{2}$ and $C_{4}D_{2}$. Units of electrons, e.

	$\partial p_z / \partial R_{\rm CH}$	$\partial p_z / \partial R_{C=C}$	
Exp. $(+-)_{\rm H}$	0.238 ± 0.006	- 0.153 ± 0.004	
$(++)_{\rm D}*$	0.238 ± 0.006	- 0.159 ± 0.007	
4-31G	0.280	- 0.122	
MNDO	0.328	- 0.423	

*(+ +)_D indicates that $\partial p_z/\partial Q_4$ and $\partial p_z/\partial Q_5$ are both positive for C₄D₂.



Fig. 2. The G intensity sum rule graph for the Π_{μ} symmetry species of diacetylene.

KOOPS et al., considering both its smaller residual error and the concordance in the signs of their dipole moment derivatives with respect to the symmetry coordinates, $\partial \mathbf{p}/\partial S_j$, with those from the propyne, was (+ +). In Fig. 2 it is readily noted that for this symmetry species also the G-sum rule graph strongly establishes the (+ +) set without using intensity data from the other symmetry species or similar chemical species.

In Table 2 are given the experimental and theoretical values of the dipole moment derivatives with respect to the internal coordinates for the Π_u symmetry species. The experimental signs of the $\partial p_x / \partial \phi_{klm}$ are identical to those obtained from the quantum chemical calculations.

Finally, the atomic polar tensors and effective charges were determined for the preferred sign choices of the diacetylene, (+-;++) for C₄H₂ and (++;++) for C₄D₂. To obtain the polar tensors, P_x, we have used the equation [7],

$$\mathbf{P}_{x} = \mathbf{P}_{R}\mathbf{B} + \mathbf{P}_{\rho}\boldsymbol{\beta} \tag{3}$$

and since diacetylene has a null dipole moment, $\mathbf{P}_{\rho}\beta = 0$, only the vibrational contribution to \mathbf{P}_{x} must be evaluated. The atomic effective charges were calculated by using the equation [7],

$$\xi_{\alpha}^{2} = \operatorname{TR}(P_{x}^{(\alpha)}P_{x}^{\prime(\alpha)}) \tag{4}$$

Table 2. Experimental and theoretical dipole moment derivatives of the Π_{μ} symmetry species of C_4H_2 and C_4D_2 . Units of electrons, e.

	$\partial p_x / \partial \phi_{\rm HCC}$	$\partial p_x / \partial \phi_{\rm CCC}$
Exp. $(++)_{\rm H}^*$ $(++)_{\rm D}$	$\begin{array}{c} 0.223 \pm 0.008 \\ 0.213 \pm 0.009 \end{array}$	0.190 + 0.005 0.192 + 0.016
4-31G MNDO	0.281 0.195	0.274 0.214

*(++)_H indicates that $\partial p_x/\partial Q_8$ and $\partial p_x/\partial Q_9$ are both positive for C₄H₂.

where $P_x^{(\alpha)}$ is the polar tensor of the α th atom. Table 3 shows the atomic polar tensors and effective charges for the diacetylene. The hydrogen effective charge calculated from Eqn. (4) ($\xi_{\rm H} = 0.369e$) is in excellent agreement with that obtained from the *G*-sum rule ($\xi_{\rm H} = 0.371e$). This value is similar to that found in other acetylenic compounds [10].

The $H(C \equiv C)_n H$ Series

In order to save the computational effort, MNDO semiempirical molecular orbital calculations were carried out on the $H(C\equiv C)_n H$ (n = 1, 2, 3, 4 and 5) series for better understanding of the effect of increasing chain length on the hydrogen atomic polar tensor. To identify more exactly the possible source that produces the APT change, we have used the charge-charge flux-overlap model (CCFO) [11]. This model applied to a hydrogen polar tensor element obtained from a molecular orbital calculation may be written as:

$$\partial p_{\sigma}/\partial \sigma_{\rm H} = q_{\rm H}^0 + \sum_{\alpha} (\partial q_{\alpha}/\partial \sigma_{\rm H}) \sigma_{\alpha}^0 + \partial p_{\sigma}'/\partial \sigma_{\rm H} \quad (5)$$

where $\sigma = x$, y or z. Here $q_{\rm H}^0$ is the equilibrium net charge of the hydrogen; the summation term represents the charge flux due to the hydrogen displacement and $\partial p'_{\sigma}/\partial \sigma_{\rm H}$ denotes the non-classical contribution. To calculate each element of the APT the numerical difference approximation $\partial p_{\sigma}/\partial \sigma_{\rm H}$ $\simeq \Delta p_{\sigma}/\Delta \sigma_{\rm H}$ was employed, with $\Delta \sigma_{\rm H} = 0.02$ Å. In Table 4 are shown the MNDO calculated values of

Table 3. Experimental atomic polar tensors and effective charges of the diacetylene. Units of electrons, e*

α	$P_{xx}^{(\alpha)} = P_{yy}^{(\alpha)}$	$P_{zz}^{(a)}$	ζa
H1	0.200	0.238	0.369
Ċ,	-0.221	- 0.394	0.503
$\tilde{C_3}$	0.021	0.156	0.159

*Atomic numbering: $H_6C_5C_4C_3C_2H_1 \rightarrow Z$.

 $\partial p_z/\partial z_H$ and $\partial p_x/\partial x_H$ for the H(C=C)_nH (n = 1, 2, 3, 4 and 5) series with their respective CCFO contributions.

MNDO values of $\partial p_z/\partial z_H$ for these molecules increase in absolute magnitude with the carbon chain length. The CCFO contributions show that these increases are due to increasing values in the charge flux contributions to $\partial p_z/\partial z_H$. This result suggests that the growth of the $\partial p_z/\partial z_H$ is mainly due to charge transfer effect along the carbon chain rather than to varying electronic structure of the hydrogen atom in these molecules. Indeed, since the $\partial p_z/\partial z_H$ element reflects principally the CH stretching, the above result is in agreement with the increasing intensity values for the CH stretchings in C_2H_2 [3] and C_4H_2 [4] i.e., 70.4 and 136.0 km · mol⁻¹, respectively.

In contrast to $\partial p_z/\partial z_H$, the $\partial p_x/\partial x_H$ element remains remarkably constant along the series and its magnitude depends mostly to the equilibrium net charge value. This invariance of the $\partial p_x/\partial x_H$ reflects the similar intensity values observed for the HCC deformations in HC₂H [3] and HC₄H [4], i.e., 177.1 and 172.0 km mol⁻¹.

Acetylenic proton acidity

The effect of the substituent on the rates of proton transfer from monosubstituted acetylenes has been the object of several studies [12]. In general, this information in the gas phase is more difficult to be obtained directly, and the same for the measure of the acetylenic intrinsic acidity. In this sense, molecular orbital calculations have contributed enormously, see Ref. [13].

On the other hand, GUSSONI *et al.* [2] have classified acid and neutral hydrogens from infrared intensity parameters. Here we have observed (see Table 5) a good correlation comparing the $\partial p_z/\partial z_H$ or $P_{ZZ}^{(H)}$ experimental element with the acetylenic intrinsic acidity calculated from *ab initio* 4-31G calculations (ΔE). According to POWELL *et al.* the theoretical intrinsic acidity is the difference between the calculated molecular energy for the parent acetylene (R-C=C-H) and the corresponding acetylenic anion (R-C=C-). The results show that the greater is $P_{ZZ}^{(H)}$

Table 4. MNDO calculated CCFO contributions to $\partial p_z/\partial z_H$ and $\partial p_x/\partial x_H$ for the HC_nH molecule. Units of electrons, e

	$\partial p_z / \partial z_H$	$(\partial p_z/\partial z_H)_{Ch.}$	$(\partial p_z/\partial z_H)_{Chflux}$	$(\partial p_z/\partial z_H)_{\rm overl.}$
HC ₂ H	0.288	0.157	0.198	-0.067
HC₄H	0.404	0.171	0.303	- 0.070
HCH	0.462	0.172	0.363	-0.073
HC ₈ H	0.502	0.173	0.404	- 0.075
HC ₁₀ H	0.531	0.173	0.436	- 0.078
	$\partial p_x / \partial x_{\rm H}$	$(\partial p_x/\partial x_{\rm H})_{Ch.}$	$(\partial p_x/\partial x_{\rm H})_{Ch{\rm flux}}$	$(\partial p_x / \partial x_H)_{\rm overl}$
HC ₂ H	0.174	0.157	0	0.017
HC₄H	0.178	0.171	0	0.007
HC ₆ H	0.178	0.172	0	0.006
HC ₈ H	0.178	0.173	0	0.005
HC10H	0.178	0.173	0	0.005

Table 5. APT's element $(P_{ZZ}^{(H)})$, 4-31G intrinsic acidity (ΔE) and rates of detritiation by hydroxide ion (K_{OH^-}) of acetylenic hydrogens

Substituent R-C=C-H	P ^{([1]} ₂₂₂ (e)	ΔE(H)*	$K_{OH^{-1}}(M^{-1}s^{-1})^{4}$
C≡N	0.267	0.5889	3.93 × 10 ⁶
C≡C–H	0.238	0.6215	
Н	0.183	0.6523	5.41×10^{1}
CH ₃	0.180	0.6595	1.50×10^{1}

*From Ref. [13].

more acid is acetylenic proton, i.e., the greater the rate of ditritiation by hydroxide ion (K_{OH} -), see Table 5. Thus, the cyanoacetylene (HC_3N) is the most acid, whereas the propyne is the least acid of them.

If this can be extended to the $H(C=C)_nH$ series, we can expect an increasing acidity along the series, since the $P_{ZZ}^{(H)}$ value increases with the carbon chain length. Thus, the greater the charge flux due to the displacement of the proton, the more acid should be the acetylenic compound.

CONCLUSIONS

G-sum rule graph and quantum chemical calculations strongly establish the $\partial \mathbf{p}/\partial Q_i$ signs, atomic polar tensors and effective charges of the diacetylene. The senses of the dipole moment changes for diacetylene are exactly those observed for other similar acetylenic compounds. The hydrogen effective charge in the diacetylene is greater than that in acetylene, as a consequence of the charge flux increasing reflected in the $P_{ZZ}^{(H)}$ element. MNDO calculations show that the increasing carbon chain length tends to increase the charge flux due to the CH stretching. However, it will be interesting to investigate the problem from more sophisticated theoretical calculations, i.e., *ab initio* 631G* calculations. Unfortunately, this goes beyond our computational facilities.

Finally, we have observed that the $P_{ZZ}^{(H)}$ element of acetylenic hydrogens can be a good indicator of its acid character, through a direct comparison with both the theoretical intrinsic acidity and the rate of detribution by hydroxide ion.

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